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## COHOMOLOGY OF LINE BUNDLES ON G/B

BY LAKSHMI BAI, C. MUSILI AND C. S. SESHADRI

(Ann. Scient. Éc. Norm. Sup., 4° série, t. 7, 1974, p. 89 à 138.)

G. Kempf has pointed out that the computation of the line bundle  $K_r$  on  $X(w_n)_r$  [cf. § 3, B, type  $B_n$ , 6, 7 (b) and 8; p. 115 to 121] is incorrect and that in fact it turns out to be the trivial line bundle. However this does not affect the proof of the main theorem of paragraph 3, Type  $B_n$  (Theorem B. 11), in fact the proof of the essentiel step I on p. 121 now becomes immediate after writing the exact cohomology sequence. Further as we shall now see, the proof that  $K_r$  is trivial also turns out to be simpler than the considerations of the paper for computing  $K_r$ .

Thus one has to make the following correction: In place of Proposition B. 9 (p. 119) one has

**PROPOSITION.**  $-K_r$  is isomorphic to the trivial line bundle and in particular, we have the exact sequence.

$$0 \to \mathcal{O}_{X(w_n)_r} \to \mathcal{O}_{Z_r} \to \mathcal{O}_{X(w_n)_r} \to 0.$$

**Proof.** - Let  $P = P_{\hat{x}}$ , T, B be the subgroups of  $G = SO(2n+1) \subseteq GL(2n+1)$ and identify  $P \setminus G$  with the quadric  $Q \equiv x_1 y_n + \ldots + x_n y_1 + z^2 = 0$  in  $P^{2n} = \{(x_1, \ldots, x_n, z, y_1, \ldots, y_n)\}$  as in the paper. The coordinate functions  $x_1, \ldots, x_n, z, y_1, \ldots, y_n$  can be canonically identified with functions on G, namely the entries of the last row. We have the ideals  $I = (x_1, \ldots, x_n, z)$  and  $J = (x_1, \ldots, x_n)$ in A = k [G]. Take the action of G on A induced by right translation. Recall that I and J are B-stable ideals. Further notice that the element z is B-*invariant* modulo J (not merely B-stable modulo J, we see that B acts on z mod J through the trivial character).

Let K = I/J as in the paper. Let R = A/I; then  $R = k [X(w_n)]$ . Since  $I^2 \subset J$ , I/J acquires a B-action consistent with the canonical B-action on R (B-actions induced by right multiplication). To prove that  $K_r$  is the trivial line bundle on  $X(w_n)_r$ , we have to show that (as R-module) I/J is B-isomorphic to R, R being considered as a module over itself. Since  $K_I$  is a line bundle, we know that I/J is a projective R-module of rank 1. Hence it suffices to show that there exists  $m \in I/J$  such that: 1° m generates I/J over R and 2° m is B-invariant. For m we take the image in I/J of  $z \in I$ . Since  $z^2 \in J$ it follows that z generates I/J over R and we have seen that z mod J is a B-invariant element.

Q. E. D.

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